## Cambridge Assessment International Education

Cambridge Ordinary Level

MATHEMATICS (SYLLABUS D)
4042/22
Paper 2
October/November 2017
MARK SCHEME
Maximum Mark: 100

## Published

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## Abbreviations

| cao | correct answer only |
| :--- | :--- |
| dep | dependent |
| FT | follow through after error |
| isw | ignore subsequent working |
| oe | or equivalent |
| SC | Special Case |
| nfww | not from wrong working <br> soi |
| seen or implied |  |


| Question | Answer | Marks | Partial Marks |
| :---: | :--- | ---: | :--- |
| 1(a) | A by 240 | $\mathbf{4}$ |  |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 2(c) | 49.3 | 3 | M1 for $(12 \times 10+28 \times 30+45 \times 50+22 \times 70+13 \times 90)$ and <br> B1 dep for their $\Sigma f x \div 120$ |
| 3(a) | $\left(\begin{array}{l}5 \\ 6 \\ 8\end{array}\right)$ cao | 1 |  |
| 3(b)(i) | $\binom{440}{540}$ cao | 2 | B1 for one element correct |
| 3(b)(ii) | The amount Anya makes for men's Tshirts and women's T-shirts | 1 |  |
| 3(c)(i) | $\left(\begin{array}{lll}290 & 630 & 537.5[0]\end{array}\right)$ | 2 | B1 for two correct values seen in a row of 3 elements or column of 3 elements isw |
| 3(c)(ii) | 48.7\% | 3 | M1FT for their $(440+540)$ and their $(290+630+$ 537.5) <br> and <br> M1 for (their 1457.5 - their 980 ) $\div$ their 980 oe |
| 4(a)(i) | Triangle $B$ at $(4,-1),(4,-4),(5,-4)$ | 2 | B1 For triangle B the correct size and orientation |
| 4(a)(ii) | Triangle $C$ at (1, 4), $(3,4)(3,-2)$ | 2 | B1 for correct size and orientation, incorrect position or for triangle with two vertices correct or for triangle at $(-3,0),(-5,0),(-5,6)$ |
| 4(b)(i) | Triangle $Q$ at (3, 1), (9, 1), (6, 3) | 2 | B1 for coordinates $(3,1),(9,1)$ and $(6,3)$ soi or for triangle with two vertices correct |
| 4(b)(ii) | (Stretch) factor 3 <br> $y$-axis invariant or parallel to $x$-axis | 2 | B1 for either |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 5(a) | $\frac{14-x}{(x-2)(x+1)}$ Final answer | 2 | M1 for $\frac{4(x+1)-5(x-2)}{(x-2)(x+1)}$ or better soi |
| 5(b) | -4 or 1.5 oe | 3 | B1 for $2 x^{2}+5 x-12[=0] \quad$ and M1 for $(2 x-3)(x+4)[=0]$ OR <br> M1 for FT factorising their 3-term quadratic equation <br> Or for correct FT substitution into formula oe and <br> A1FT for solutions from their quadratic equation |
| 5(c)(i) | $\begin{aligned} & 3 p+2 n=4.8[0] \text { or } 3 p+2 n=480 \\ & 5 p+4 n=9[.00] \text { or } 5 p+4 n=900 \end{aligned}$ | 1 |  |
| 5(c)(ii) | $\begin{aligned} & 0.6[0] \\ & 1.5[0] \end{aligned}$ | 3FT | M1 for a correct method to eliminate one variable <br> A1 for either $p=0.6[0]$ or $n=1.5[0]$ www <br> After A0, B1FT for a correct substitution to find the other variable <br> After 0, SC1 for a pair of values that satisfy either equation |
| 6(a)(i) | 1 | 1 |  |
| 6(a)(ii) | $10,12,14,15,16,18,20$ | 1 |  |
| 6(a)(iii) | $\frac{7}{11} \mathrm{oe}$ | 1 |  |
| 6(b)(i) | 8 | 2 | M1 for $14+10+24-x=40$ oe or for correct Venn diagram with algebraic expressions. <br> Or B1 for Venn diagram with at least 3 numbers correct |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 6(b)(ii) | $\frac{28}{45} \text { oe }$ | 2FT | M1 for $\frac{\text { their } 8}{k} \times \frac{\text { their } 7}{k-1}[\times 2] \quad$ where $k>$ their 8 Or $\mathbf{S C 1}$ for $\left(\frac{\text { their } 8}{10}\right)^{2}$ |
| 7(a)(i) | -4.5-4.5 | 1 | Both correct |
| 7(a)(ii) | Correct smooth curve | 3FT | B2FT for 8 or 9 points correctly plotted Or B1FT for 6 or 7 points correctly plotted Or $\mathbf{B 1}$ for the correct scales drawn |
| 7(a)(iii) | -2.4 to -1.6 dependent on tangent drawn | 2 | Accept a correctly formed $\Delta y \div \Delta x$ isw <br> B1 for tangent drawn at $(3,1.5)$ |
| 7(a)(iv)(a) | -2 cao |  |  |
| 7(a)(iv)(b) | -2.4 to -2.3 and 4.3 to 4.4 |  | FT reading their graph at $y=$ their -2 Tolerance $\pm 1$ small square <br> B1 FT for one correct |
| 7(b)(i) | 4 | 1 |  |
| 7(b)(ii) | 3 | 1 |  |
| 7(b)(iii) | 324 | 1 |  |
| 8(a)(i) | $\begin{aligned} & \frac{y}{2} \text { oe } \\ & \text { angle at centre }=\text { twice angle at } \\ & \text { circumference oe } \end{aligned}$ | 2 | $\mathbf{B} 1 \text { for } \frac{y}{2}$ |
| 8(a)(ii) | $90-y \text { oe }$ <br> [Angle between] radius and tangent $=90^{\circ}$, <br> [sum of angles in a triangle] | 2 | B1 for $90-y$ |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 8(a)(iii) | $2 y$ oe <br> or $2(90$ - their (a)(ii)) <br> or 180-2 their (a)(ii) <br> Angle in semicircle $=90^{\circ}$ | 2FT | FT dependent on expressions in $y$ <br> B1 for $2 y$ |
| 8(b) | EFC | 1 |  |
| 8(c) | Any two of <br> - $\angle O C G$ is common oe <br> - $\angle A D C=\angle O G C\left[=90^{\circ}\right]$ <br> - $\angle D A C=\angle G O C[=y]$ <br> with no incorrect reason or fact stated | 2 | B1 for one pair of angles |
| 8(d) | Trapezium | 1 |  |
| 8(e)(i) | 1:4 oe | 1 |  |
| 8(e)(ii) | 1:8 oe | 1 |  |
| 9(a) | 7.54 | 2 | M1 for $\pi \times 0.4^{2} \times 15$ |
| 9(b) | 53.7 | 4 | M1 for $\frac{1}{2} \times 4.5^{2} \times \sin 110$ oe M1 for $\frac{250}{360} \times \pi \times 4.5^{2}$ or $\frac{110}{360} \times \pi \times 4.5^{2}$ M1 for their $9.514+$ their 44.18 oe |
| 9(c) | 2 minutes 20 seconds | 2 | M1 for figs $175 \div 45$ soi |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 9(d) | $146.5^{\circ}$ | 4 | B3 for $33.5^{\circ}$ <br> Or <br> M2 for $\sin Q=\frac{450 \sin 62}{720} \quad$ Or <br> M1 for $\frac{\sin Q}{450}=\frac{\sin 62}{720}$ <br> AND <br> M1 for 180 - their $Q$ |
| 10(a) | $3 x^{2}+16 x-460=0$ correctly derived | 4 | B1 for $(x+4)(3 x+4)$ oe and <br> M1 for expanding brackets and collecting like terms <br> and <br> M1 for their area $=476$ <br> and <br> A1 for correct simplification leading to $3 x^{2}+16 x-460=0$ |
| 10(b) | $10 \text { and }-\frac{46}{3} \text { oe }(-15.3)$ | 3 | B2 for $(x-10)(3 x+46)$ <br> Or <br> M1 for such as $(x+a)(3 x+b)$ with $a b=-460$ or $3 a+b=16$ <br> A1FT for solutions from their factors |
| 10(c) | $\begin{aligned} & {[\text { Height }=] 14} \\ & {[\text { Length }=] 34} \end{aligned}$ | 2FT | B1FT for either, or for both correct but in the wrong places |
| 10(d) | 61.6 or $16($ their + ve root +1$) \times 0.35$ | 3FT | M2 for (their 476 - their $10 \times$ their 30$) \times 0.5 \times 0.7$ oe Or M1 for their 476 - their $10 \times$ their 30 oe |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 11(a) | Need to see 2.58 rounded from a correctly obtained 2581 or better. | 3 | Method 1 <br> M2 for $A Y=3.65 \cos 45$ or $(3.65 \div 2) \div \sin 45$ or <br> M1 for e.g. $\frac{A Y}{3.65}=\cos 45$ or $\sin 45=\frac{3.65 \div 2}{A Y}$ <br> Method 2 <br> M1 for such as $A Y^{2}+A Y^{2}=3.65^{2}$ or $3.65^{2}+3.65^{2}=A C^{2}$ soi <br> M1 for $A Y^{2}=\frac{3.65^{2}}{2}$ oe <br> A1 for $A Y=2.580[9 \ldots]$ |
| 11(b) | 7.93 | 2 | M1 for $7.5^{2}+2.58^{2}$ |
| 11(c) | $26.6^{\circ} \text { or } 2 \sin ^{-1}\left(\frac{0.5 \times 3.65}{\text { their } 7.93}\right)$ | 3FT | M2 for $2 \sin ^{-1}\left(\frac{0.5 \times 3.65}{\text { their } 7.93}\right)$ <br> or $\cos [\ldots]=\frac{\text { their } 7.93^{2}+\text { their } 7.93^{2}-3.65^{2}}{2 \times \text { their } 7.93^{2}}$ <br> Or <br> M1 for $\sin [\ldots]=\frac{0.5 \times 3.65}{\text { their } 7.93}$ <br> or $3.65^{2}=$ their $7.93^{2}+$ their $7.93^{2}-2 \times$ their $7.93^{2} \times$ $\cos [\ldots]$ |
| 11(d)(i) | 11.18 or 11.2 | 2 | M1 for $\tan 77=\frac{X Y}{2.58}$ oe |
| 11(d)(ii) | $80.7^{\circ}$ | 2FT | M1 for $\tan [\ldots]=\frac{\text { their } 11.2}{3.65 \div 2}$ |

