

MATHEMATICS (SYLLABUS D)

4042/22 October/November 2017

Paper 2 MARK SCHEME

Maximum Mark: 100

Published

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Abbreviations

| cao dep FT | correct answer only dependent follow through after error |
|------------------|--|
| isw | ignore subsequent working |
| oe | or equivalent |
| SC | Special Case |
| nfww | not from wrong working |
| soi | seen or implied |

| Question | Answer | Marks | Partial Marks |
|----------|------------------------------------|-------|---|
| 1(a) | A by 240 | 4 | |
| | | | B3 for 4980 and 5220 seen or difference = 240 Or |
| | | | M1 for 4500 ÷ 5 and 12 × 340 oe and |
| | | | M1 for 0.12 × 4500 and 24 × 195 oe and |
| | | | M1 for the difference between <i>their</i> 5220 and <i>their</i> 4980 |
| 1(b) | 10.61 cao | 3 | |
| | | | M2 for 240 ÷ 100 × 5.2 × 0.85 soi Or |
| | | | M1 for 240 ÷ 100 × 5.2 or <i>their</i> 12.48 × 0.85 or 5.2 × 0.85 |
| 1(c) | 42 | 3 | |
| | | | B2 for 280 Or |
| | | | M1 for $1.15 x = 322$ soi and |
| | | | M1 for 322 – <i>their</i> 280 |
| 2(a)(i) | 12 40 85 107 | 1 | |
| 2(a)(ii) | Correct cumulative frequency curve | 2 | |
| | | | B1FT for at least 5 correct plots |
| 2(b)(i) | 47 to 49 | 1FT | |
| 2(b)(ii) | 28 to 32 | 2FT | |
| | | | B1 for 63 to 65 or 32 to 35 |

| Question | Answer | Marks | Partial Marks |
|----------|---|-------|---|
| 2(c) | 49.3 | 3 | |
| | | | M1 for (12×10 + 28×30 + 45×50 + 22×70 + 13×90) |
| | | | and |
| | | | B1 dep for <i>their</i> $\Sigma fx \div 120$ |
| 3(a) | $\begin{pmatrix} 5\\6\\8 \end{pmatrix}$ cao | 1 | |
| 3(b)(i) | $\begin{pmatrix} 440\\540 \end{pmatrix}$ cao | 2 | |
| | | | B1 for one element correct |
| 3(b)(ii) | The amount Anya makes for men's T- shirts and women's T-shirts | 1 | |
| 3(c)(i) | (290 630 537.5[0]) | 2 | |
| | | | B1 for two correct values seen in a row of 3 elements or column of 3 elements isw |
| 3(c)(ii) | 48.7% | 3 | |
| | | | M1FT for <i>their</i> (440 + 540) and <i>their</i> (290 + 630 + 537.5) and |
| | | | M1 for (<i>their</i> 1457.5 – <i>their</i> 980) ÷ <i>their</i> 980 oe |
| 4(a)(i) | Triangle <i>B</i> at (4, -1), (4, -4), (5, -4) | 2 | |
| | | | B1 For triangle B the correct size and orientation |
| 4(a)(ii) | Triangle C at $(1, 4), (3, 4) (3, -2)$ | 2 | |
| | | | B1 for correct size and orientation, incorrect position or for triangle with two vertices correct or for triangle at (-3, 0), (-5, 0), (-5, 6) |
| 4(b)(i) | Triangle <i>Q</i> at (3, 1), (9, 1), (6, 3) | 2 | |
| | | | B1 for coordinates (3, 1), (9, 1) and (6, 3) soi or for triangle with two vertices correct |
| 4(b)(ii) | (Stretch) factor 3 | 2 | |
| | <i>y</i> -axis invariant or parallel to <i>x</i> -axis | | |
| | | | B1 for either |

| Question | Answer | Marks | Partial Marks |
|-----------|--|-------|--|
| 5(a) | $\frac{14-x}{(x-2)(x+1)}$ Final answer | 2 | |
| | | | M1 for $\frac{4(x+1)-5(x-2)}{(x-2)(x+1)}$ or better soi |
| 5(b) | -4 or 1.5 oe | 3 | |
| | | | B1 for $2x^2 + 5x - 12 = 0$] and |
| | | | M1 for $(2x-3)(x+4) = 0$ |
| | | | OR |
| | | | M1 for FT factorising their 3-term quadratic equation |
| | | | Or for correct FT substitution into formula oe |
| | | | and |
| | | | A1FT for solutions from their quadratic equation |
| 5(c)(i) | 3p + 2n = 4.8[0] or $3p + 2n = 4805p + 4n = 9[.00]$ or $5p + 4n = 900$ | 1 | |
| 5(c)(ii) | 0.6[0] 1.5[0] | 3FT | |
| | | | M1 for a correct method to eliminate one variable |
| | | | A1 for either $p = 0.6[0]$ or $n = 1.5[0]$ www |
| | | | After $A0$, $B1FT$ for a correct substitution to find the other variable |
| | | | After 0 , SC1 for a pair of values that satisfy either equation |
| 6(a)(i) | 1 | 1 | |
| 6(a)(ii) | 10, 12, 14, 15, 16, 18, 20 | 1 | |
| 6(a)(iii) | $\frac{7}{11}$ oe | 1 | |
| 6(b)(i) | 8 | 2 | |
| | | | M1 for $14 + 10 + 24 - x = 40$ oe or for correct Venn diagram with algebraic expressions. Or B1 for Venn diagram with at least 3 numbers correct |

| Question | Answer | Marks | Partial Marks |
|-------------|---|-------|---|
| 6(b)(ii) | $\frac{28}{45}$ oe | 2FT | |
| | 45 | | |
| | | | M1 for $\frac{their 8}{k} \times \frac{their 7}{k-1} [\times 2]$ where $k >$ their 8 |
| | | | Or SC1 for $\left(\frac{their 8}{10}\right)^2$ |
| 7(a)(i) | -4.5 -4.5 | 1 | Both correct |
| 7(a)(ii) | Correct smooth curve | 3FT | |
| | | | B2FT for 8 or 9 points correctly plotted |
| | | | Or B1FT for 6 or 7 points correctly plotted |
| | | | Or B1 for the correct scales drawn |
| 7(a)(iii) | -2.4 to -1.6 dependent on tangent drawn | 2 | Accept a correctly formed $\Delta y \div \Delta x$ isw |
| | | | B1 for tangent drawn at (3, 1.5) |
| 7(a)(iv)(a) | -2 cao | | |
| 7(a)(iv)(b) | -2.4 to -2.3 and 4.3 to 4.4 | | FT reading their graph at $y = their -2$ Tolerance ± 1 small square |
| | | | B1 FT for one correct |
| 7(b)(i) | 4 | 1 | |
| 7(b)(ii) | 3 | 1 | |
| 7(b)(iii) | 324 | 1 | |
| 8(a)(i) | $\frac{y}{2}$ oe | 2 | |
| | 2 angle at centre = twice angle at circumference oe | | |
| | | | B1 for $\frac{y}{2}$ |
| 8(a)(ii) | 90 – <i>y</i> oe | 2 | |
| | [Angle between] radius and tangent = 90° , | | |
| | [sum of angles in a triangle] | | B1 for 90 – <i>y</i> |

| Question | Answer | Marks | Partial Marks |
|-----------|--|-------|--|
| 8(a)(iii) | 2y oe or 2(90 - their (a)(ii)) or 180 - 2 their (a)(ii) Angle in semicircle = 90° | 2FT | FT dependent on expressions in <i>y</i> |
| | | | B1 for 2 <i>y</i> |
| 8(b) | EFC | 1 | |
| 8(c) | Any two of • $\angle OCG$ is common oe • $\angle ADC = \angle OGC$ [= 90°] • $\angle DAC = \angle GOC$ [= y] with no incorrect reason or fact stated | 2 | B1 for one pair of angles |
| 8(d) | Trapezium | 1 | |
| 8(e)(i) | 1 : 4 oe | 1 | |
| 8(e)(ii) | 1 : 8 oe | 1 | |
| 9(a) | 7.54 | 2 | |
| | | | M1 for $\pi \times 0.4^2 \times 15$ |
| 9(b) | 53.7 | 4 | |
| | | | M1 for $\frac{1}{2} \times 4.5^2 \times \sin 110$ oe |
| | | | M1 for $\frac{250}{360} \times \pi \times 4.5^2$ or $\frac{110}{360} \times \pi \times 4.5^2$ |
| | | | M1 for <i>their</i> 9.514 + <i>their</i> 44.18 oe |
| 9(c) | 2 minutes 20 seconds | 2 | |
| | | | M1 for figs 175 ÷ 45 soi |

| Question | Answer | Marks | Partial Marks |
|----------|--|-------|--|
| 9(d) | 146.5° | 4 | |
| | | | B3 for 33.5° Or |
| | | | |
| | | | M2 for $\sin Q = \frac{450 \sin 62}{720}$ Or |
| | | | M1 for $\frac{\sin Q}{450} = \frac{\sin 62}{720}$ AND |
| | | | M1 for 180 – <i>their Q</i> |
| 10(a) | $3x^2 + 16x - 460 = 0$ correctly derived | 4 | |
| | | | B1 for $(x+4)(3x+4)$ oe and |
| | | | M1 for expanding brackets and collecting like terms and |
| | | | M1 for <i>their</i> area = 476 and |
| | | | A1 for correct simplification leading to $3x^2 + 16x - 460 = 0$ |
| 10(b) | 10 and $-\frac{46}{3}$ oe (-15.3) | 3 | |
| | | | B2 for $(x - 10)(3x + 46)$ Or |
| | | | M1 for such as $(x+a)(3x+b)$ with $ab = -460$ or $3a + b = 16$ |
| | | | A1FT for solutions from their factors |
| 10(c) | [Height =] 14 [Length =] 34 | 2FT | |
| | | | B1FT for either, or for both correct but in the wrong places |
| 10(d) | 61.6 or 16(their +ve root + 1)×0.35 | 3FT | |
| | | | M2 for (<i>their</i> $476 - their 10 \times their 30$) $\times 0.5 \times 0.7$ oe |
| | | | Or M1 for <i>their</i> $476 - their 10 \times their 30$ oe |

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| Question | Answer | Marks | Partial Marks |
|-------------------|---|------------|---|
| 11(a) | Answer Need to see 2.58 rounded from a correctly obtained 2 581 or better. | Marks 3 | Method 1 M2 for $AY = 3.65 \cos 45$ or $(3.65 \div 2) \div \sin 45$ or M1 for e.g. $\frac{AY}{3.65} = \cos 45$ or $\sin 45 = \frac{3.65 \div 2}{AY}$ Method 2 M1 for such as $AY^2 + AY^2 = 3.65^2$ or $3.65^2 + 3.65^2 = AC^2$ soi M1 for $AY^2 = \frac{3.65^2}{2}$ oe A1 for $AY = 2.580[9]$ |
| 11(b) | 7.93 | 2 | M1 for $7.5^2 + 2.58^2$ |
| 11(c) 11(d)(i) | 26.6° or $2\sin^{-1}\left(\frac{0.5 \times 3.65}{their 7.93}\right)$ 11.18 or 11.2 | 3FT 2 | M2 for $2\sin^{-1}\left(\frac{0.5 \times 3.65}{their7.93}\right)$ or $\cos\left[\dots\right] = \frac{their7.93^2 + their7.93^2 - 3.65^2}{2 \times their7.93^2}$ Or M1 for $\sin[\dots] = \frac{0.5 \times 3.65}{their7.93}$ or $3.65^2 = their7.93^2 + their7.93^2 - 2 \times their 7.93^2 \times \cos\left[\dots\right]$ |
| 11(a)(1) | 11.18 OF 11.2 | 2 | M1 for $\tan 77 = \frac{XY}{2.58}$ oe |
| 11(d)(ii) | 80.7° | 2FT | M1 for tan $[] = \frac{their 11.2}{3.65 \div 2}$ |